# From D-Branes to M-Branes: Up from String Theory

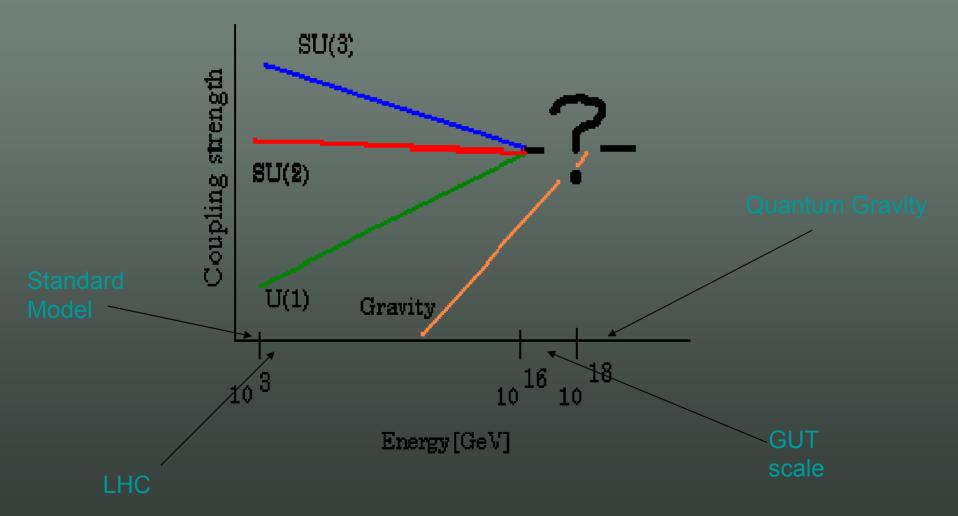
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## Plan

- Introduction
- What is String Theory?
- D-branes
- M-Theory
- M-branes
- Conclusions

## The World (as seen from CERN)

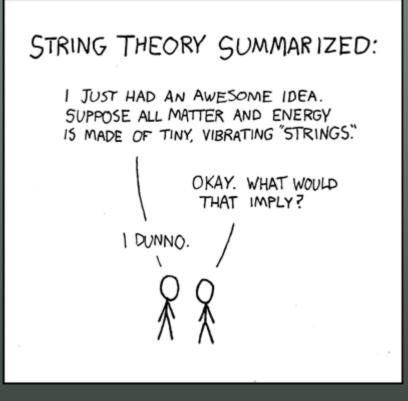


- The Standard Model of particle physics is incredibly successful
  - Describes structure and interactions of all matter from deep inside nucleons upwards
- General Relativity is also very successful
  - Describes physics on large to cosmologically large scales
- But they are famously hard to reconcile
  - GR is classical
  - Standard Model is an effective low-energy theory

\* Well maybe 20% of it

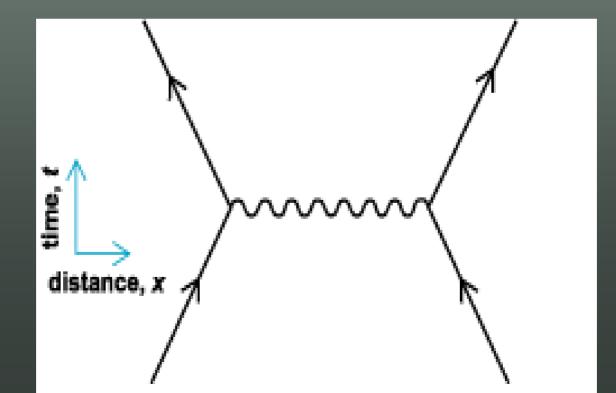
- String Theory seems capable of describing all that we expect in one consistent framework:
  - Quantum Mechanics and General Covariance
  - Standard Model-like gauge theory
  - General Relativity
  - Cosmology (inflation)?

# What is String Theory?

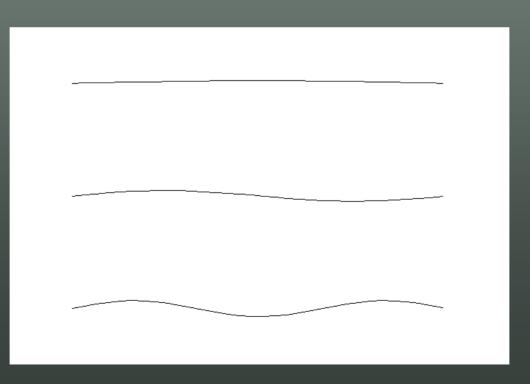


Well in fact we know an awful lot (although not what string theory really is)

- (perturbative) quantum field theory assumes that the basic states are pointlike particles
  - Interactions occur when two particles meet:

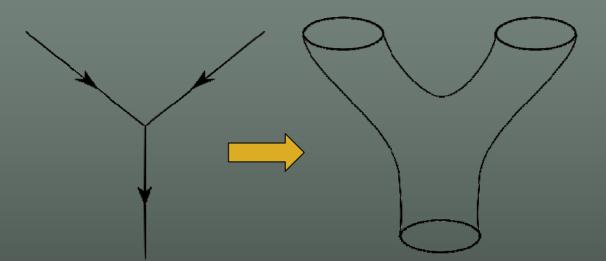


- Point particles are replaced by 1dimensional strings
  - Multitude of particles correspond to the lowest harmonics of an infinite tower of modes





 Feynman diagrams merge and become smooth surfaces



• Only one coupling constant: g<sub>s</sub>

- Vacuum expectation value of a scalar field – the dilaton

- A remarkable feature is that gravity comes out of the quantum theory, unified with gauge forces
- The dimension of spacetime is 10
  - Must compactify to 4D
  - There appear to be a plethora of models with Standard Model-like behaviour

– Estimated 10<sup>500</sup> 4D vacua

Landscape

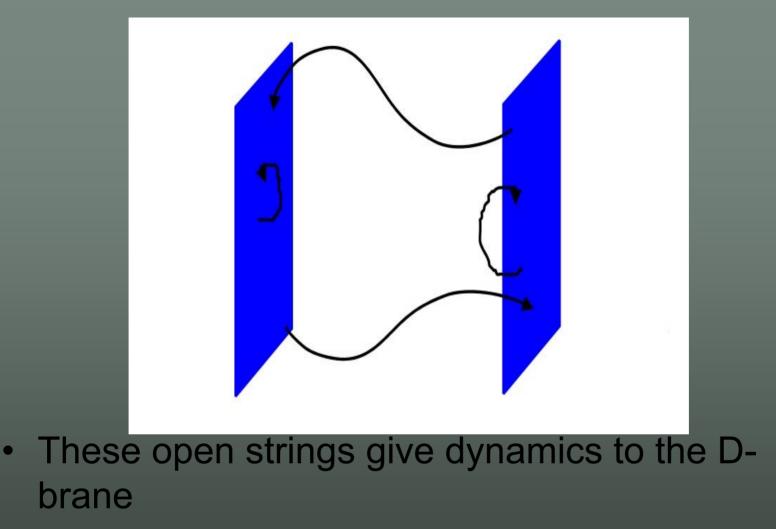
# The World (as seen from the Multiverse)



# **D-Branes**

- In addition to strings, String Theory contains D-branes:
  - p-dimensional surfaces in spacetime
    - 0-brane = point particle
    - 1-brane = string
    - 2-brane = membrane
    - *etc....*

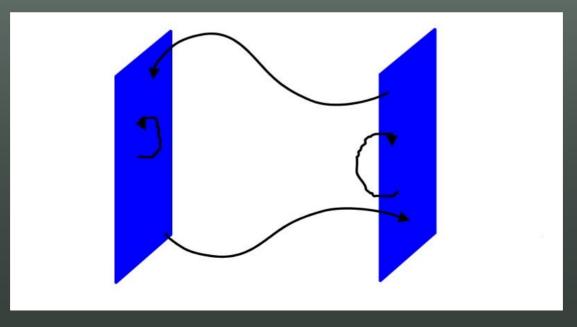
Non-perturbative states: Mass ~ 1/g<sub>s</sub>
 End point of open strings



 At lowest order the dynamics are those of U(n) Super-Yang-Mills

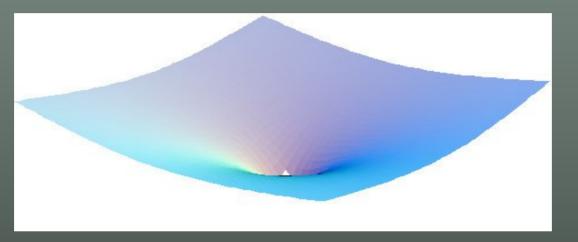
### $-\,g_{\rm YM}$ is determined from $g_{\rm s}$

- Light modes on the worldvolume arise from the open strings (Higg's mechanism)
  - Mass = length of a stretched string between the branes
- Vast applications to model building



• At low energy D-branes appear as (extremal) charged black hole solutions

Singularity is extended along p-dimensions



- Thus D-branes have both a Yang-Mills description as well as a gravitational one
  - Exact counting of black hole microstates
  - AdS/CFT

# What is M-Theory?

- But not all is perfect in String Theory
  - Are there really 10<sup>500</sup> vacua?
  - Can one make any observable predictions?
- What is String Theory really?
  - The construction of vibrating interacting strings is just a perturbative device, not a definition of the theory
    - What are strongly coupled strings?
- Furthermore why 5 perturbative string theories
  - Type I
  - Type II A & B
  - Heterotic  $E_8 x E_8 \& SO(32)$

 Now all 5 are all thought to be related as different aspects of single theory:

# **M-theory**

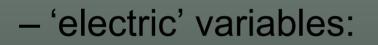
• How?

# Duality

Two theories are dual if they describe the same physics but with different variables.
 e.g. S-duality g<sub>s</sub> ↔ 1/g<sub>s</sub>



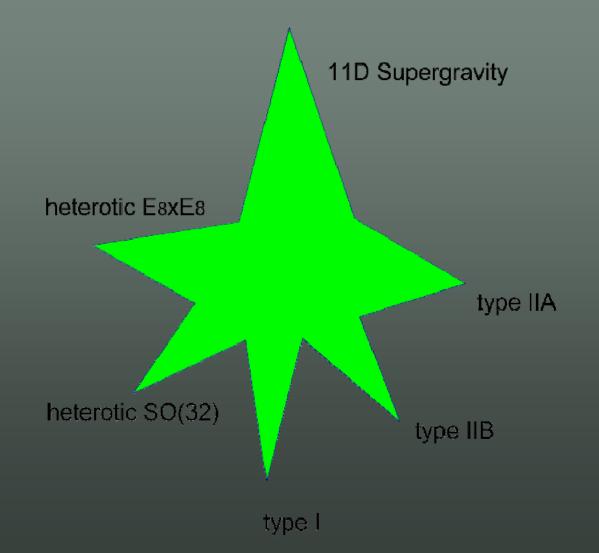
• The classic example of duality occurs in Maxwell's equations without sources:



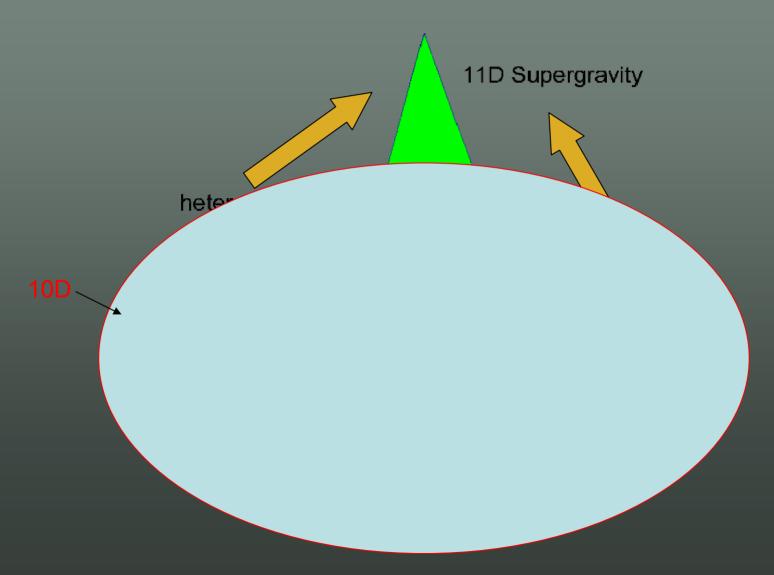
- 'magnetic' variables:

Self-dual

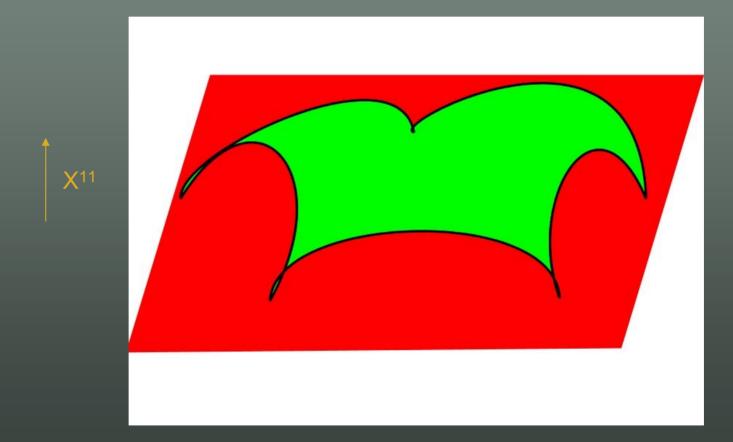
• M-theory moduli space:



• M-theory moduli space: at strong coupling



• M-theory moduli space in 3D:



### -

• An 11D metric tensor becomes a 10D metric tensor plus a vector and a scalar

U(1) gauge field

Scalar that controls the size of the 11<sup>th</sup> dimension

- Thus the String Theory dilaton has a geometric interpretation as the size of the 11<sup>th</sup> dimension
  - But the vev of  $is g_s$
  - String perturbation theory is an expansion about a degenerate 11<sup>th</sup> dimension
  - $As g_s \rightarrow \infty$  an extra dimension opens up
    - 11D theory in the infinite coupling limit.
- Predicts a complete quantum theory in eleven dimensions: M-Theory
  - Effective action is 11D supergravity
  - Little else is known

# **M-Branes**

### Type IIA String Theory

0-Branes

Strings

2-branes

4-branes

5-branes

6-Branes

M-Theory

gravitational wave along X<sup>11</sup>

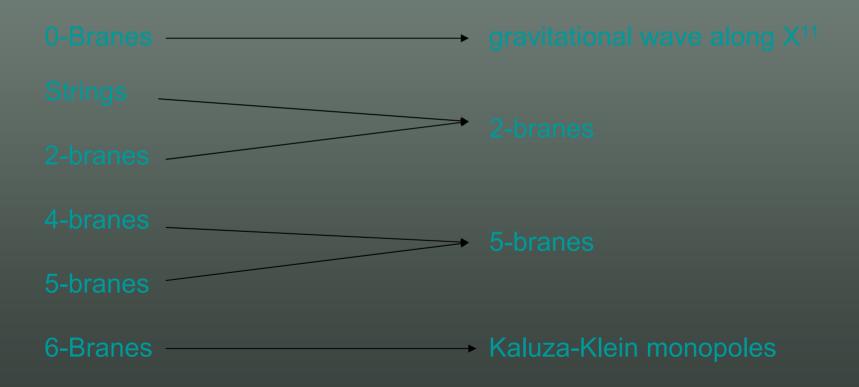
2-branes

5-branes

Kaluza-Klein monopoles

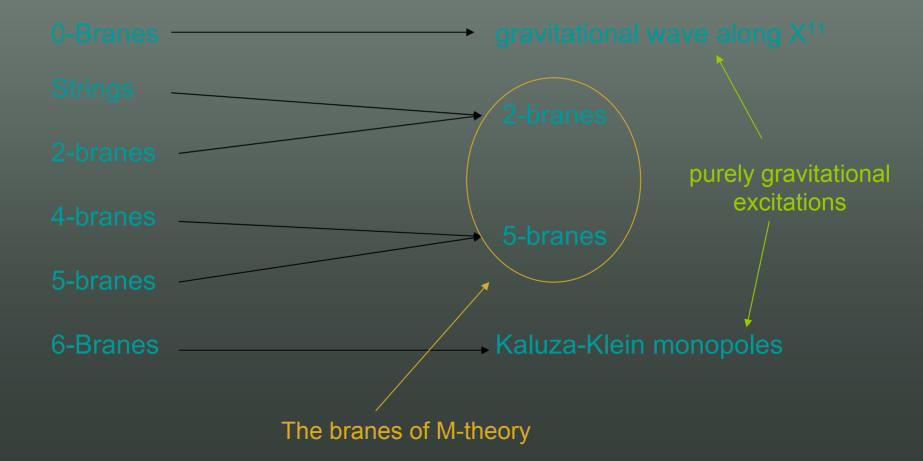
# **M-Branes**

### Type IIA String TheoryM-Theory



# **M-Branes**

### Type IIA String TheoryM-Theory



- So there are no strings in M-theory
   2-branes and 5-branes
- In particular no open strings and no g<sub>s</sub>
  - No perturbative expansion
  - No microscopic understanding
- The dynamics of a single M-branes act to minimize their worldvolumes
  - With other fields related by supersymmetry
    - M2 [Bergshoeff, Sezgin, Townsend]
    - M5 [Howe, Sezgin, West]
- What about multiple M-branes?

- In string theory you can derive the dynamics of multiple D-branes from symmetries:
  - Effective theory has 16 supersymmetries and breaks SO(1,9) → SO(1,p) × SO(9-p)
  - This is in agreement with maximally supersymmetric Yang-Mills gauge theory

- Can we derive the dynamics of M2-branes from symmetries?
  - Conformal field theory
    - Strong coupling (IR) fixed point of 3D SYM
  - No perturbation expansion
  - The only maximally supersymmetric Lagrangians are Yang-Mills theories
    - Wrong symmetries for M-Theory
    - need SO(1,2) x SO(8) not SO(1,2) x SO(7)

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Wrong symmetries for M-Theory

need SO(1,2) x SO(8) not SO(1,2) x SO(7)

• Well that turns out not to be true

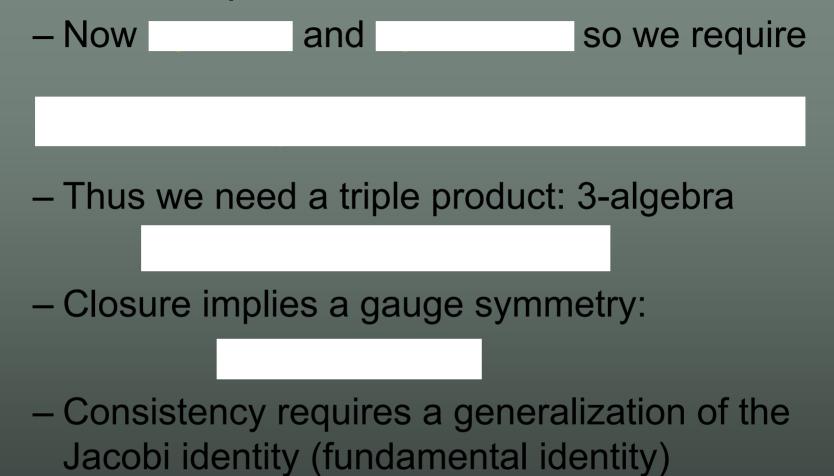
- The Yang-Mills theories living on D-branes are determined by the susy variation

• Here we find a Lie-algebra with a bi-linear antisymmetric product:

• Closure of the susy algebra leads to gauge symmetry:

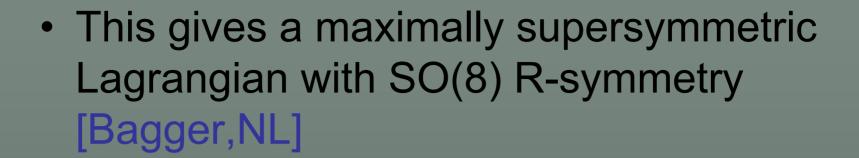
• Consistency of this implies the Jacobi identity:

• What is required for M2-branes?



### The fundamental identity implies the gauge symmetry acts as a (non simple) Lie algebra acting on

 3-algebra data is equivalent to specifying a Lie-algebra with a (split) metric and a representation acting on vector space space (with an invariant metric).



### 'twisted' Chern-Simons gauge theory

• Conformal, parity invariant

• But it turns out to only have one example:



- SU(2)xSU(2) Chern-Simons at level (k,-k) and matter in the bi-fundamental
- Vacuum moduli space:

Two M2-branes in R<sup>8</sup>/Z<sub>2</sub>
 – agrees with M-theory when k=2

- Need to generalize:
  - Weak coupling arises from orbifold
  - Consider  $C^4/Z_k$

- 12 susys and breaks SO(8)  $\rightarrow$  SU(4)xU(1) • Look for theories with SU(4)xU(1) R-
- symmetry and N=6 supersymmetry

- From the 3-algebra this is achieved if the triple product is no longer totally anti-symmetric:

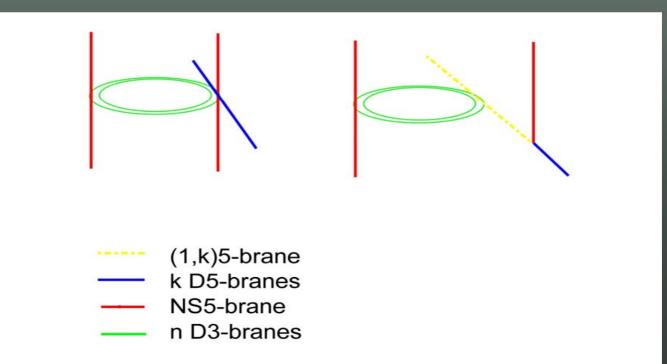
X,Y,Z are Complex Scalar Fields

- Consistency requires a related fundamental identity
- For example we can take (for nxm matrices):

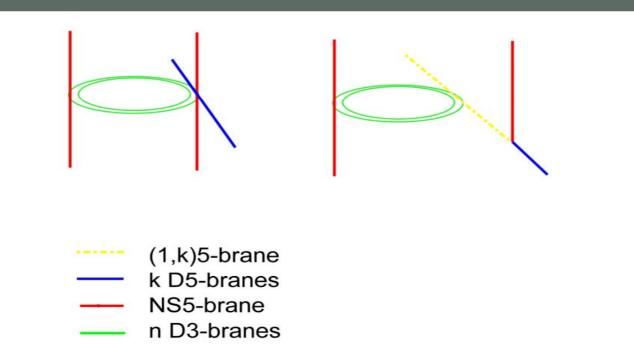
- Resulting action is similar to the N=8 case but:
  - U(n)xU(m) Chern-Simons theory at level (k,-k) with matter in the bifundamental

- These theories were was first proposed by [Aharony, Bergman, Jafferis and Maldacena]
- They gave a brane diagram derivation

   Consider the following Hannay-Witten picture



- In terms of the D3-brane SYM worldvolume theory:
  - Integrating out D5/D3-strings and flowing to
     IR gives a U(n)×U(n) CS theory with level (k,k) coupled to bi-fundamental matter
  - N=3 is enhanced to N=6





• The final configuration is just n M2s in a curved background preserving 3/16 susys.

- Metric can be written explicitly

- smooth except where the centre's intersect
- near horizon limit gives n M2's in R<sup>8</sup>/Z<sub>k</sub>.
- Preserved susy's are enhanced to 6/16.
- Note that this works for all n and all k
   even k=1,2 where we expect N=8 susy
  - Two supersymmetries are not realized in the Lagrangian (carry U(1) charge)
  - For k=1 even the centre of mass mode is obscured

 One success of these models is an understanding of the mysterious n<sup>3/2</sup> growth of the degrees of freedom

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- Free energy = f(\lambda)n^2

• \lambda = n/k

• f(\lambda) = \begin{cases} 1 & \lambda <<1 \\ & \lambda^{-1/2} & \lambda >>1 \end{cases}
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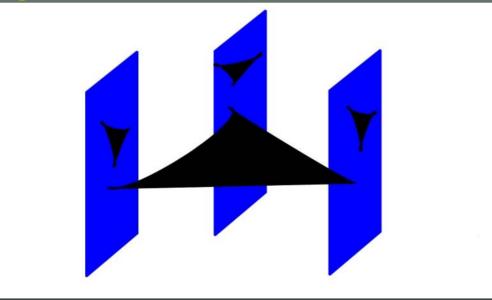
 This has recently been confirmed in Chern-Simons Theory for all λ [Drukker, Marino, Putrov]

- How does one recover D2-branes from this [Mukhi, Papageorgakis]

- Give a vev to a scalar field
  - breaks  $U(n)xU(n) \rightarrow U(n)$  and  $SO(8) \rightarrow SO(7)$

- becomes a dynamical U(n) gauge field
  - Similar to a Higg's effect where a non-dynamical vector eats a scalar to become dynamical

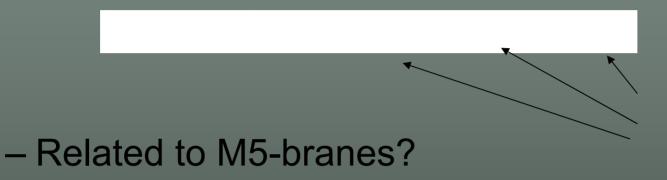
- What can we learn about M-theory?
   Hints at microscopic dynamics of M-branes
  - e.g. in the N=8 theory one finds mass = area of a triangle with vertices on an M2



- Mass deformations give fuzzy vacua:

- M2-branes blow up into fuzzy M5-branes
- Can we learn about M5-branes
  - Also M2s can end on M5's: Chern-Simons gauge fields become dynamical

- There are also infinite dimensional totally antisymmetric 3-algebras: Nambu bracket



Functions on a 3-manifold

- Infinitely many totally anti-symmetric 3algebras with a Lorentzian metric
  - Seem to be equivalent to 3D N=8 SYM but with manifest SO(8) and conformal symmetry

# Conclusions

- M-Theory and M-branes are poorly understood but there has been much recent progress:
  - Complete proposal for the effective Lagrangian of n M2's in  $\ensuremath{\mathsf{R}^8/\mathsf{Z}_k}$
  - Novel highly supersymmetric Chern-Simons gauge theories based on a 3-algebra.
  - Gives a Lagrangian description of strongly coupled 3D super Yang-Mills
- M5-branes remain very challenging as does M-Theory itself but hopefully progress will be made

- M2-brane CFT's 'define' M-theory in  $AdS_4xX_7$